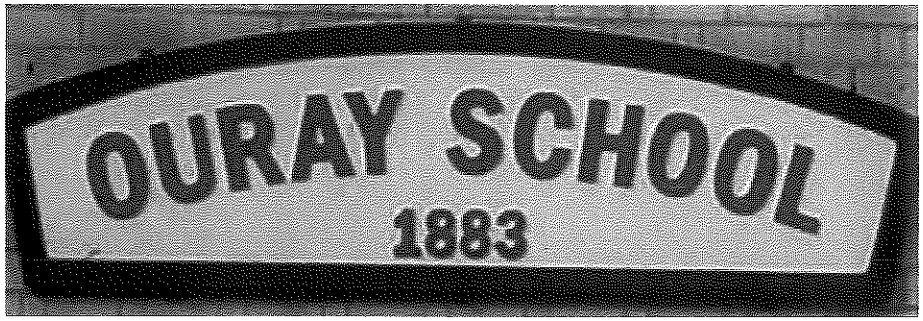
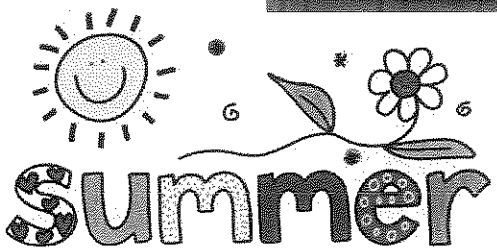
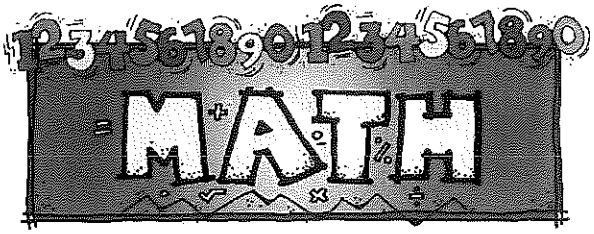






For students entering:

ALGEBRA II

Name: _____

- ➔ Turn in completed packet on the **first day of the school year.**
- ➔ All work must be shown in the packet OR on separate paper.
- ➔ This packet will be graded – start off the year with a 100%.
- ➔ Expect a test on this material during the first week of school.

OURAY HIGH SCHOOL
Summer Review Packet

This packet has been designed to provide a review of pre-requisite skills that are essential for student success in mathematics next year. This packet contains review material of the algebraic concepts, skills, and procedures that should be mastered **prior** to entering Algebra II in the fall. Students are expected to complete this booklet during the summer and bring it, with work shown, on the first day of school. A test assessing mastery of these skills will be given on the first week of school.

Below are some online resources that you might find useful for extra review:

Khan Academy: http://www.khanacademy.org/
IXL: http://www.ixl.com/math

Algebra I Textbook (UCSMP):
https://sites.google.com/a/bonnyeagle.org/brodiemath/ucsmp-algebra/course-materials

Geometry Textbook Resources (Discovering Geometry):
http://math.kendallhunt.com/x19356.html

Algebra II Textbook (Discovering Advanced Algebra):
http://hsebooks.kendallhunt.com/DAA/ebook/daa.html?userid=48651

Algebra II Textbook (Larson):
https://sites.google.com/a/gaston.k12.nc.us/jcsmithweb/home/textbook-pdf

If you have any questions, feel free to e-mail me at arosenberg@ouray.k12.co.us. I will not be checking my e-mail during certain periods of the summer, but I will definitely check in from time to time and get back to you.

Keep your brain in shape this summer by practicing your math and logic skills. And, brush up on the skills in this packet so that you start of the year feeling confident and strong! You can do it!

Miss Angela Rosenberg

Algebra 1 Skills Needed to be Successful in Algebra 2

A. Simplifying Polynomial Expressions

Objectives: The student will be able to:

- Apply the appropriate arithmetic operations and algebraic properties needed to simplify an algebraic expression.
- Simplify polynomial expressions using addition and subtraction.
- Multiply a monomial and polynomial.

B. Solving Equations

Objectives: The student will be able to:

- Solve multi-step equations.
- Solve a literal equation for a specific variable, and use formulas to solve problems.

C. Rules of Exponents

Objectives: The student will be able to:

- Simplify expressions using the laws of exponents.
- Evaluate powers that have zero or negative exponents.

D. Binomial Multiplication

Objectives: The student will be able to:

- Multiply two binomials.

E. Factoring

Objectives: The student will be able to:

- Identify the greatest common factor of the terms of a polynomial expression.
- Express a polynomial as a product of a monomial and a polynomial.
- Find all factors of the quadratic expression $ax^2 + bx + c$ by factoring and graphing.

F. Radicals

Objectives: The student will be able to:

- Simplify radical expressions.

G. Graphing Lines

Objectives: The student will be able to:

- Identify and calculate the slope of a line.
- Graph linear equations using a variety of methods.
- Determine the equation of a line.

H. Regression and Use of the Graphing Calculator

Objectives: The student will be able to:

- Draw a scatter plot, find the line of best fit, and use it to make predictions.
- Graph and interpret real-world situations using linear models.

A. Simplifying Polynomial Expressions

I. Combining Like Terms

- You can add or subtract terms that are considered "like", or terms that have the same variable(s) with the same exponent(s).

Ex. 1: $5x - 7y + 10x + 3y$

$\underline{5x} \; \underline{-\,7y} + \underline{10x} + \underline{3y}$

$15x - 4y$

Ex. 2: $-8h^2 + 10h^3 - 12h^2 - 15h^3$

$\underline{-8h^2} + \underline{10h^3} \; \underline{-\,12h^2} \; \underline{-\,15h^3}$

$-20h^2 - 5h^3$

II. Applying the Distributive Property

- Every term inside the parentheses is multiplied by the term outside of the parentheses.

Ex. 1: $3(9x-4)$

$3 \cdot 9x - 3 \cdot 4$

$27x - 12$

Ex. 2: $4x^2(5x^3 + 6x)$

$4x^2 \cdot 5x^3 + 4x^2 \cdot 6x$

$20x^5 + 24x^3$

III. Combining Like Terms AND the Distributive Property (Problems with a Mix!)

- Sometimes problems will require you to distribute AND combine like terms!!

Ex. 1: $3(4x-2)+13x$

$3 \cdot 4x - 3 \cdot 2 + 13x$

$12x - 6 + 13x$

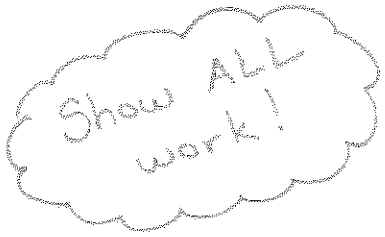
$25x - 6$

Ex. 2: $3(12x-5) - 9(-7+10x)$

$3 \cdot 12x - 3 \cdot 5 - 9(-7) - 9(10x)$

$36x - 15 + 63 - 90x$

$-54x + 48$



PRACTICE SET 1

Simplify.

1. $8x - 9y + 16x + 12y$

2. $14y + 22 - 15y^2 + 23y$

3. $5n - (3 - 4n)$

4. $-2(11b - 3)$

5. $10q(16x + 11)$

6. $-(5x - 6)$

7. $3(18z - 4w) + 2(10z - 6w)$

8. $(8c + 3) + 12(4c - 10)$

9. $9(6x - 2) - 3(9x^2 - 3)$

10. $-(y - x) + 6(5x + 7)$

Use space below for work ☺

B. Solving Equations

I. Solving Two-Step Equations

A couple of hints:

1. To solve an equation, UNDO the order of operations and work in the reverse order.
2. REMEMBER! Addition is "undone" by subtraction, and vice versa. Multiplication is "undone" by division, and vice versa.

Ex. 1: $4x - 2 = 30$

$+2 \quad +2$

$4x = 32$

$\div 4 \quad \div 4$

$x = 8$

Ex. 2: $87 = -11x + 21$

$-21 \qquad -21$

$66 = -11x$

$\div -11 \quad \div -11$

$-6 = x$

II. Solving Multi-step Equations With Variables on Both Sides of the Equal Sign

- When solving equations with variables on both sides of the equal sign, be sure to get all terms with variables on one side and all the terms without variables on the other side.

Ex. 3: $8x + 4 = 4x + 28$

$-4 \qquad -4$

$8x = 4x + 24$

$-4x \quad -4x$

$4x = 24$

$\div 4 \quad \div 4$

$x = 6$

III. Solving Equations that need to be simplified first

- In some equations, you will need to combine like terms and/or use the distributive property to simplify each side of the equation, and then begin to solve it.

Ex. 4: $5(4x - 7) = 8x + 45 + 2x$

$20x - 35 = 10x + 45$

$-10x \qquad -10x$

$10x - 35 = 45$

$+35 \quad +35$

$10x = 80$

$\div 10 \quad \div 10$

$x = 8$

PRACTICE SET 2

Solve each equation. You must show all work.

1. $5x - 2 = 33$
2. $140 = 4x + 36$
3. $8(3x - 4) = 196$
4. $45x - 720 + 15x = 60$
5. $132 = 4(12x - 9)$
6. $198 = 154 + 7x - 68$
7. $-131 = -5(3x - 8) + 6x$
8. $-7x - 10 = 18 + 3x$
9. $12x + 8 - 15 = -2(3x - 82)$
10. $-(12x - 6) = 12x + 6$

IV. Solving Literal Equations

- A literal equation is an equation that contains more than one variable.
- You can solve a literal equation for one of the variables by getting that variable by itself (isolating the specified variable).

Ex. 1: $3xy = 18$, Solve for x.

$$\frac{3xy}{3y} = \frac{18}{3y}$$

$$x = \frac{6}{y}$$

Ex. 2: $5a - 10b = 20$, Solve for a.

$$+10b = +10b$$

$$5a = 20 + 10b$$

$$\frac{5a}{5} = \frac{20}{5} + \frac{10b}{5}$$

$$a = 4 + 2b$$

PRACTICE SET 3

Solve each equation for the specified variable.

1. $Y + V = W$, for V

2. $9wr = 81$, for w

3. $2d - 3f = 9$, for f

4. $dx + t = 10$, for x

5. $P = (g - 9)180$, for g

6. $4x + y - 5h = 10y + u$, for x

C. Rules of Exponents

Multiplication: Recall $(x^m)(x^n)=x^{(m+n)}$ *Ex:* $(3x^4y^2)(4xy^5)=(3\cdot 4)(x^4\cdot x^1)(y^2\cdot y^5)=12x^5y^7$

Division: Recall $\frac{x^m}{x^n}=x^{(m-n)}$ *Ex:* $\frac{42m^5j^2}{-3m^3j}=\left(\frac{42}{-3}\right)\left(\frac{m^5}{m^3}\right)\left(\frac{j^2}{j^1}\right)=-14m^2j$

Powers: Recall $(x^m)^n = x^{(m\cdot n)}$ *Ex:* $(-2a^3bc^4)^3 = (-2)^3(a^3)^3(b^1)^3(c^4)^3 = -8a^9b^3c^{12}$

Power of Zero: Recall $x^0 = 1,\ x \neq 0$ *Ex:* $5x^0y^4 = (5)(1)(y^4) = 5y^4$

PRACTICE SET 4

Simplify each expression.

1. $(c^5)(c)(c^2)$
2. $\frac{m^{15}}{m^3}$
3. $(k^4)^5$
4. d^0
5. $(p^4q^2)(p^7q^5)$
6. $\frac{45y^3z^{10}}{5y^3z}$
7. $(-t^7)^3$
8. $3f^3g^0$
9. $(4h^5k^3)(15k^2h^3)$
10. $\frac{12a^4b^6}{36ab^2c}$
11. $(3m^2n)^4$
12. $(12x^2y)^0$
13. $(-5a^2b)(2ab^2c)(-3b)$
14. $4x(2x^2y)^0$
15. $(3x^4y)(2y^2)^3$

D. Binomial Multiplication

I. Reviewing the Distributive Property

The distributive property is used when you want to multiply a single term by an expression.

Ex 1: $8(5x^2 - 9x)$

$8 \cdot 5x^2 + 8 \cdot (-9x)$

$40x^2 - 72x$

II. Multiplying Binomials – the FOIL method

When multiplying two binomials (an expression with <u>two</u> terms), we use the "FOIL" method. The "FOIL" method uses the distributive property <u>twice</u>!

FOIL is the order in which you will multiply your terms.

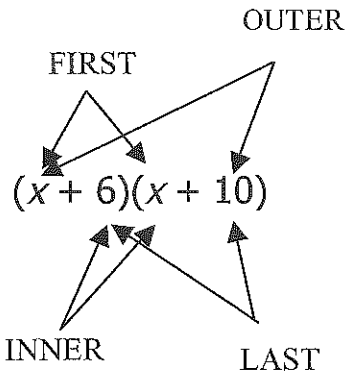
First

Outer

Inner

Last

Ex. 1: $(x + 6)(x + 10)$



First $x \cdot x$ ------> x^2

Outer $x \cdot 10$ -----> $10x$

Inner $6 \cdot x$ ------> $6x$

Last $6 \cdot 10$ -----> 60

$x^2 + 10x + 6x + 60$

$x^2 + 16x + 60$

(After combining like terms)

Recall: $4^2 = 4 \cdot 4$

$x^2 = x \cdot x$

Ex. $(x + 5)^2$

$(x + 5)^2 = (x + 5)(x+5)$

Now you can use the "FOIL" method to get a simplified expression.

PRACTICE SET 5

Multiply. Write your answer in simplest form.

1. $(x + 10)(x - 9)$
2. $(x + 7)(x - 12)$
3. $(x - 10)(x - 2)$
4. $(x - 8)(x + 81)$
5. $(2x - 1)(4x + 3)$
6. $(-2x + 10)(-9x + 5)$
7. $(-3x - 4)(2x + 4)$
8. $(x + 10)^2$
9. $(-x + 5)^2$
10. $(2x - 3)^2$

E. Factoring

I. Using the Greatest Common Factor (GCF) to Factor.

- Always determine whether there is a greatest common factor (GCF) first.

Ex. 1 $3x^4 - 33x^3 + 90x^2$

- In this example the GCF is $3x^2$.
- So when we factor, we have $3x^2(x^2 - 11x + 30)$.
- Now we need to look at the polynomial remaining in the parentheses. Can this trinomial be factored into two binomials? In order to determine this make a list of all of the factors of 30.

30		30	
1	30	-1	-30
2	15	-2	-15
3	10	-3	-10
5	6	-5	-6

Since $-5 + -6 = -11$ and $(-5)(-6) = 30$ we should choose -5 and -6 in order to factor the expression.

- The expression factors into $3x^2(x-5)(x-6)$

Note: Not all expressions will have a GCF. If a trinomial expression does not have a GCF, proceed by trying to factor the trinomial into two binomials.

II. Applying the difference of squares: $a^2 - b^2 = (a-b)(a+b)$

Ex. 2 $4x^3 - 100x$

$4x(x^2 - 25)$

$4x(x-5)(x+5)$

Since x^2 and 25 are perfect squares separated by a subtraction sign, you can apply the difference of two squares formula.

PRACTICE SET 6

Factor each expression.

1. $3x^2 + 6x$

2. $4a^2b^2 - 16ab^3 + 8ab^2c$

3. $x^2 - 25$

4. $n^2 + 8n + 15$

5. $g^2 - 9g + 20$

6. $d^2 + 3d - 28$

7. $z^2 - 7z - 30$

8. $m^2 + 18m + 81$

9. $4y^3 - 36y$

10. $5k^2 + 30k - 135$

F. Radicals

To simplify a radical, we need to find the greatest perfect square factor of the number under the radical sign (the radicand) and then take the square root of that number.

Ex. 1: $\sqrt{72}$

$\sqrt{36}\cdot\sqrt{2}$

$6\sqrt{2}$

Ex. 2: $4\sqrt{90}$

$4\cdot\sqrt{9}\cdot\sqrt{10}$

$4\cdot 3\cdot\sqrt{10}$

$12\sqrt{10}$

Ex. 3: $\sqrt{48}$

$\sqrt{16}\sqrt{3}$

$4\sqrt{3}$

OR

Ex. 3: $\sqrt{48}$

$\sqrt{4}\sqrt{12}$

$2\sqrt{12}$

This is not simplified completely because 12 is divisible by 4 (another perfect square)

$2\sqrt{4}\sqrt{3}$

$2\cdot 2\cdot\sqrt{3}$

$4\sqrt{3}$

PRACTICE SET 7

Simplify each radical.

1. $\sqrt{121}$
2. $\sqrt{90}$
3. $\sqrt{175}$
4. $\sqrt{288}$
5. $\sqrt{486}$
6. $2\sqrt{16}$
7. $6\sqrt{500}$
8. $3\sqrt{147}$
9. $8\sqrt{475}$
10. $\sqrt{\frac{125}{9}}$

G. Graphing Lines

I. Finding the Slope of the Line that Contains each Pair of Points.

Given two points with coordinates (x_1, y_1) and (x_2, y_2), the formula for the slope, m, of the line containing the points is $m = \frac{y_2 - y_1}{x_2 - x_1}$.

Ex. (2, 5) and (4, 1)

$m = \frac{1-5}{4-2} = \frac{-4}{2} = -2$

The slope is -2.

Ex. (-3, 2) and (2, 3)

$m = \frac{3-2}{2-(-3)} = \frac{1}{5}$

The slope is $\frac{1}{5}$

PRACTICE SET 8

1. (-1, 4) and (1, -2)

2. (3, 5) and (-3, 1)

3. (1, -3) and (-1, -2)

4. (2, -4) and (6, -4)

5. (2, 1) and (-2, -3)

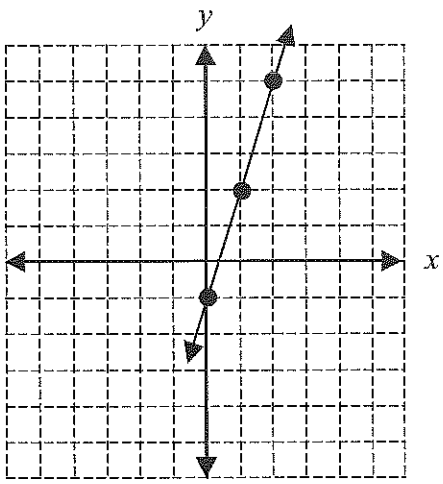
6. (5, -2) and (5, 7)

II. Using the Slope – Intercept Form of the Equation of a Line.

The slope-intercept form for the equation of a line with slope m and y-intercept b is $y = mx + b$.

Ex. $y = 3x - 1$

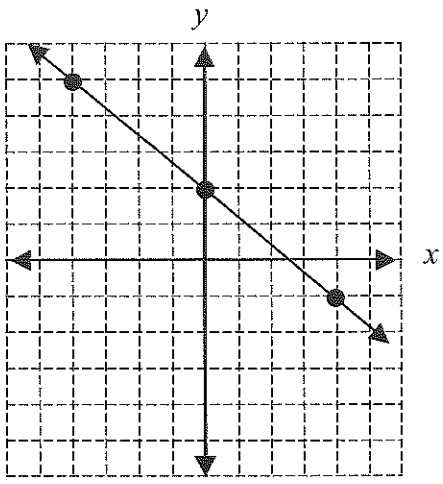
Slope: 3 y-intercept: -1



Place a point on the y-axis at -1. Slope is 3 or 3/1, so travel up 3 on the y-axis and over 1 to the right.

Ex. $y = -\frac{3}{4}x + 2$

Slope: $-\frac{3}{4}$ y-intercept: 2

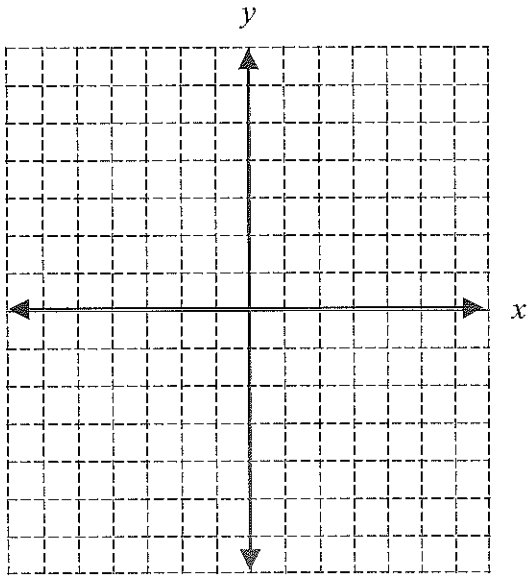


Place a point on the y-axis at 2. Slope is -3/4 so travel down 3 on the y-axis and over 4 to the right. Or travel up 3 on the y-axis and over 4 to the left.

PRACTICE SET 9

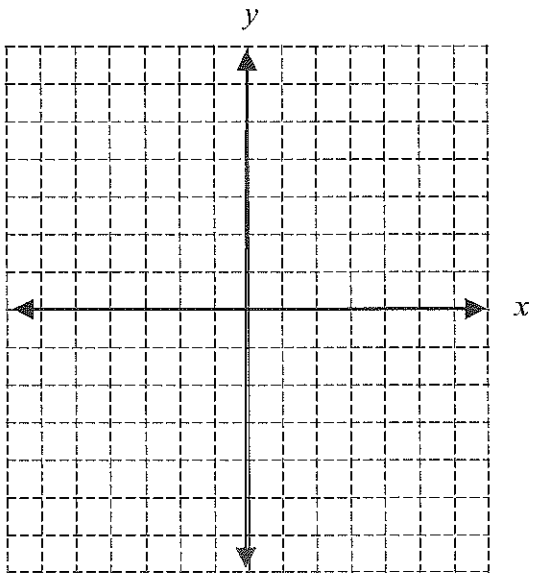
1. $y = 2x + 5$

Slope: _____ y-intercept: _____



2. $y = \frac{1}{2}x - 3$

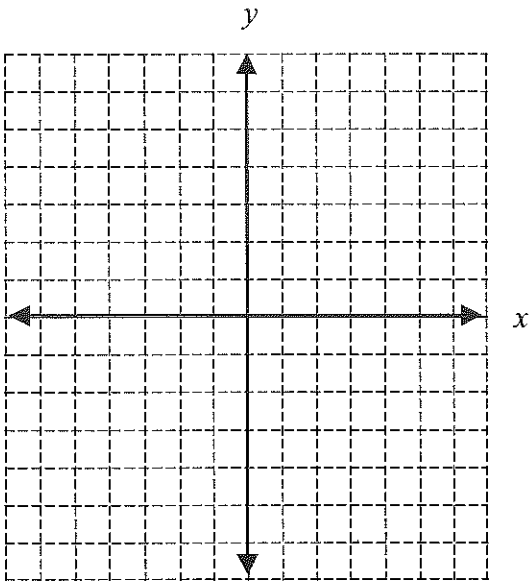
Slope: _____ y-intercept: _____



3. $y = -\frac{2}{5}x + 4$

Slope: _____

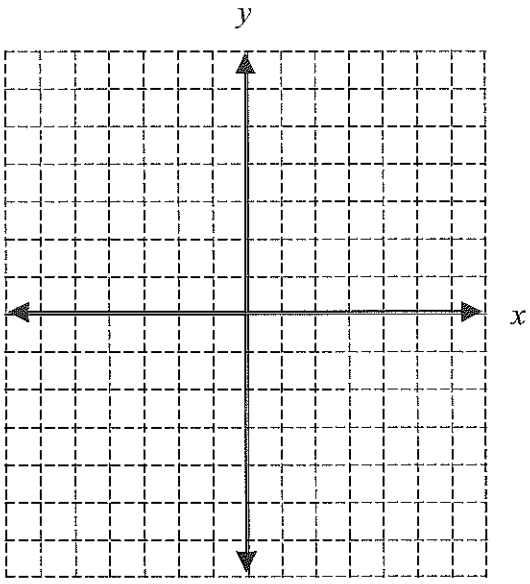
y-intercept: _____



4. $y = -3x$

Slope: _____

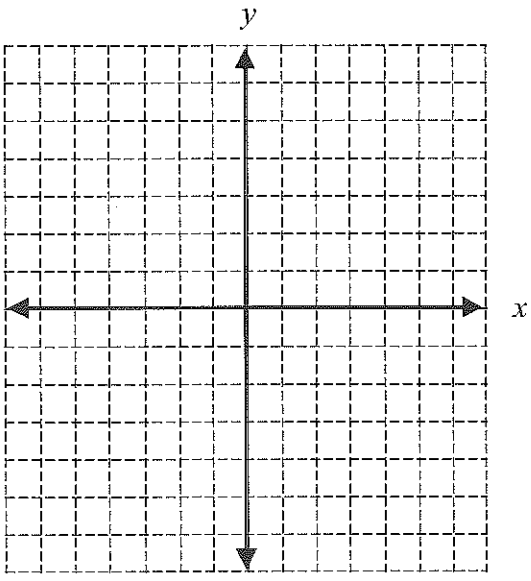
y-intercept _____



5. $y = -x + 2$

Slope: _____

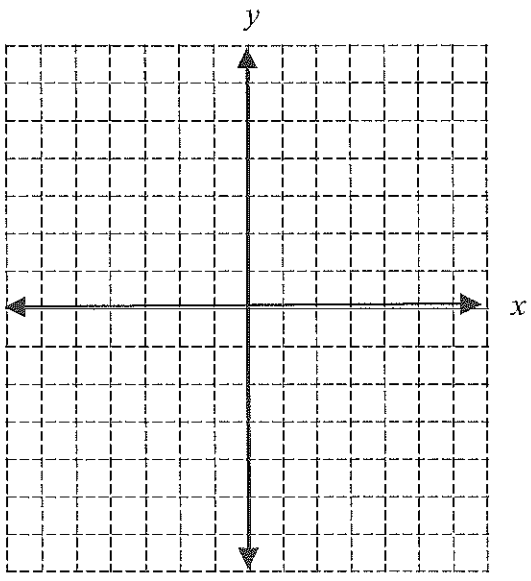
y-intercept: _____



6. $y = x$

Slope: _____

y-intercept _____



III. Using Standard Form to Graph a Line.

An equation in standard form can be graphed using several different methods. Two methods are explained below.

a. Re-write the equation in $y = mx + b$ form, identify the y-intercept and slope, then graph as in Part II above.

b. Solve for the x- and y- intercepts. To find the x-intercept, let $y = 0$ and solve for x. To find the y-intercept, let $x = 0$ and solve for y. Then plot these points on the appropriate axes and connect them with a line.

Ex. $2x - 3y = 10$

a. Solve for y.

$-3y = -2x + 10$

$y = \dfrac{-2x + 10}{-3}$

$y = \dfrac{2}{3}x - \dfrac{10}{3}$

OR

b. Find the intercepts:

let $y = 0$:

$2x - 3(0) = 10$

$2x = 10$

$x = 5$

So x-intercept is (5, 0)

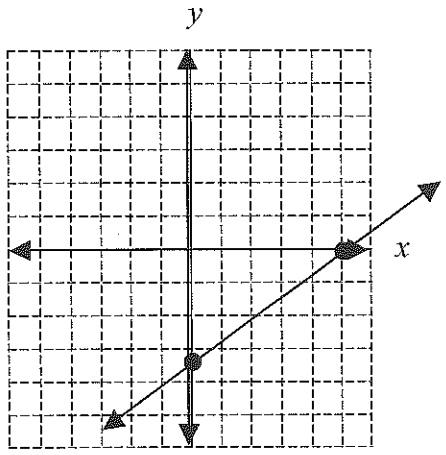
let $x = 0$:

$2(0) - 3y = 10$

$-3y = 10$

$y = -\dfrac{10}{3}$

So y-intercept is $\left(0, -\dfrac{10}{3}\right)$



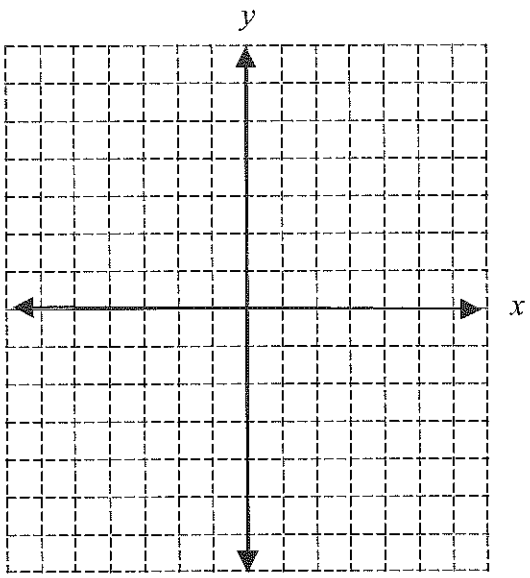
On the x-axis place a point at 5.

On the y-axis place a point at $-\dfrac{10}{3} = -3\dfrac{1}{3}$

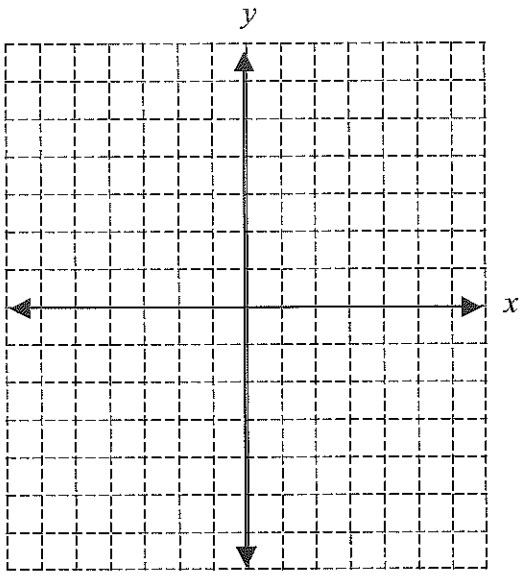
Connect the points with the line.

PRACTICE SET 10

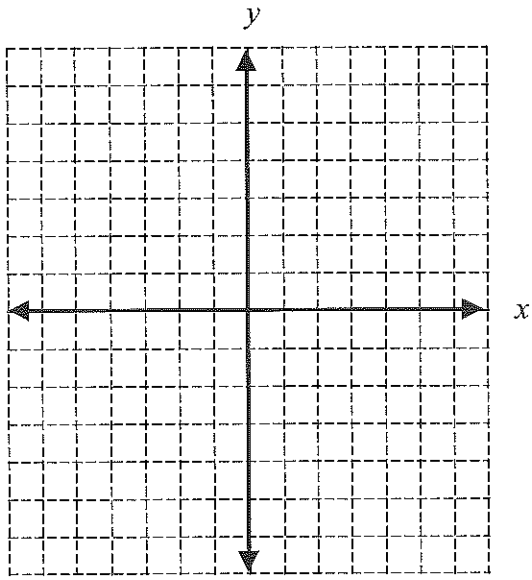
1. $3x + y = 3$



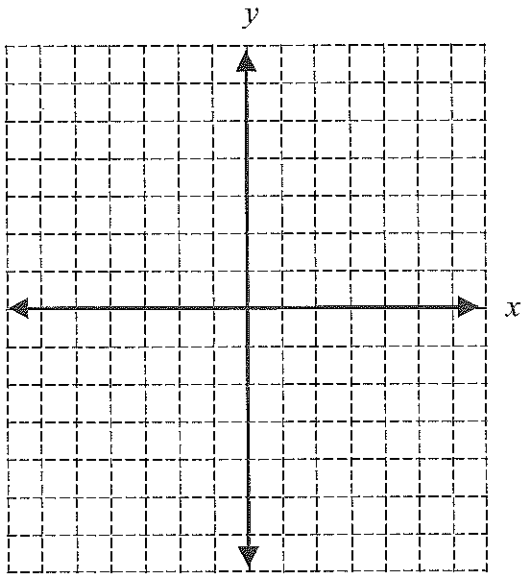
2. $5x + 2y = 10$



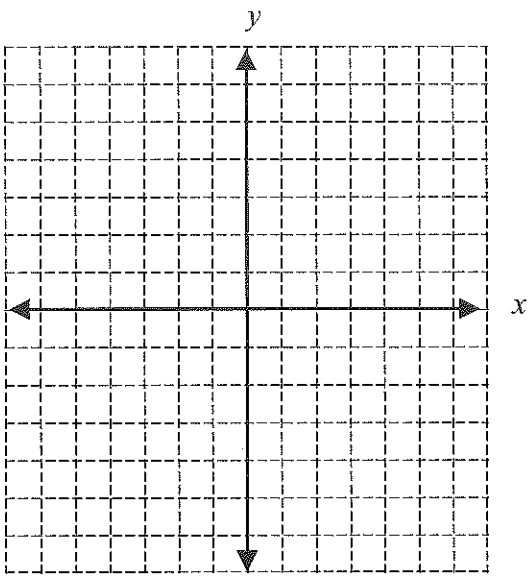
3. $y = 4$



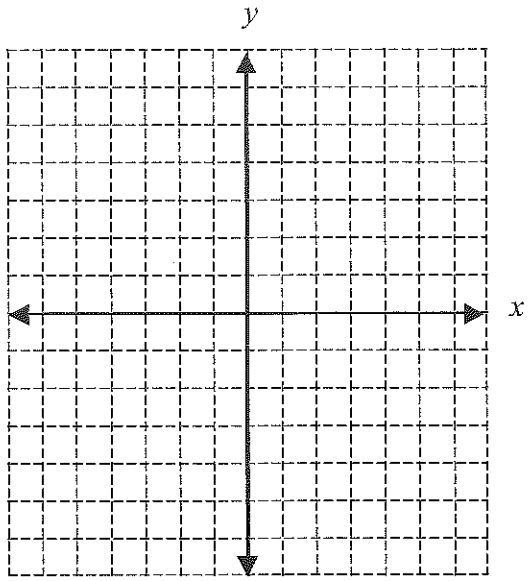
4. $4x - 3y = 9$



5. $-2x + 6y = 12$



6. $x = -3$



H. Regression and Use of the Graphing Calculator

Note: For guidance in using your calculator to graph a scatterplot and finding the equation of the linear regression (line of best fit), please see the calculator direction sheet included in the back of the review packet.

PRACTICE SET 11

1. The following table shows the math and science test scores for a group of ninth graders.

Math Test Scores	60	40	80	40	65	55	100	90	85
Science Test Scores	70	35	90	50	65	40	95	85	90

Let's find out if there is a relationship between a student's math test score and his or her science test score.

a. Fill in the table below. Remember, the variable quantities are the two variables you are comparing, the lower bound is the minimum, the upper bound is the maximum, and the interval is the scale for each axis.

Variable Quantity	Lower Bound	Upper Bound	Interval

b. Create the scatter plot of the data on your calculator.

c. Write the equation of the line of best fit.

d. Based on the line of best fit, if a student scored an 82 on his math test, what would you expect his science test score to be? Explain how you determined your answer. Use words, symbols, or both.

e. Based on the line of best fit, if a student scored a 53 on his science test, what would you expect his math test score to be? Explain how you determined your answer. Use words, symbols, or both.

2. Use the chart below of winning times for the women's 200-meter run in the Olympics below to answer the following questions.

Year	Time (Seconds)
1964	23.00
1968	22.50
1972	22.40
1976	22.37
1980	22.03
1984	21.81
1988	21.34
1992	21.81

a. Fill in the table below. Remember, the variable quantities are the two variables you are comparing, the lower bound is the minimum, the upper bound is the maximum, and the interval is the scale for each axis.

Variable Quantity	Lower Bound	Upper Bound	Interval

b. Create a scatter plot of the data on your calculator.

c. Write the equation of the regression line (line of best fit) below. Explain how you determined your equation.

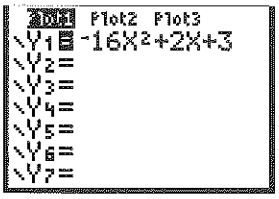
d. The Summer Olympics will be held in London, England, in 2012. According to the line of best fit equation, what would be the winning time for the women's 200-meter run during the 2012 Olympics? Does this answer make sense? Why or why not?

TI-83 Plus/TI-84 Graphing Calculator Tips

How to ...

...graph a function

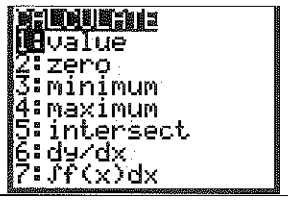
Press the [Y=] key, Enter the function directly using the [X,T,θ,n] key to input *x*. Press the [GRAPH] key to view the function. Use the [WINDOW] key to change the dimensions



and scale of the graph. Pressing [TRACE] lets you move the cursor along the function with the arrow keys to display exact coordinates.

...find the y-value of any x-value

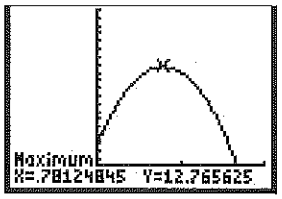
Once you have graphed the function, press **CALC** [2nd] [TRACE] and select **1:value**. Enter the *x*-value. The corresponding *y*-value is displayed and the cursor



moves to that point on the function.

...find the maximum value of a function

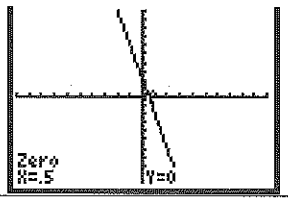
Once you have graphed the function, press **CALC** [2nd] [TRACE] and select **4:maximum**. You can set the left and right boundaries of the area to be examined and guess the maximum value either by entering values



directly or by moving the cursor along the function and pressing [ENTER]. The *x*-value and *y*-value of the point with the maximum *y*-value are then displayed.

...find the zero of a function

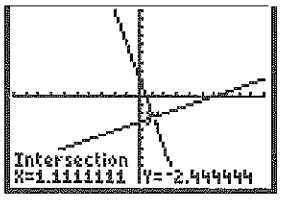
Once you have graphed the function, press **CALC** [2nd] [TRACE] and select **2:zero**. You can set the left and right boundaries of the root to be examined and guess the value either by entering values



directly or by moving the cursor along the function and pressing [ENTER]. The *x*-value displayed is the root.

...find the intersection of two functions

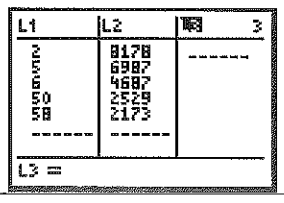
Once you have graphed the function, press **CALC** [2nd] [TRACE] and select **5:intersect**. Use the up and down arrows to move among functions and press [ENTER] to select two. Next,



enter a guess for the point of intersection or move the cursor to an estimated point and press [ENTER]. The *x*-value and *y*-value of the intersection are then displayed.

...enter lists of data

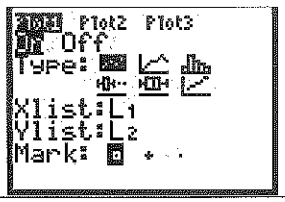
Press the [STAT] key and select **1:Edit**. Store ordered pairs by entering the *x* coordinates in **L1** and the *y* coordinates in **L2**. You can calculate new lists. To



create a list that is the sum of two previous lists, for example, move the cursor onto the **L3** heading. Then enter the formula **L1+L2** at the **L3** prompt.

...plot data

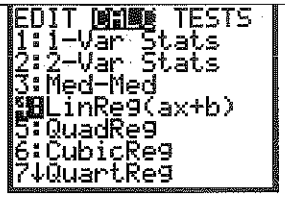
Once you have entered your data into lists, press **STAT PLOT** 2nd Y= and select **Plot1**. Select On and choose the type of graph you want, e.g. scatterplot (points not connected) or connected dot for



two variables, histogram for one variable. Press ZOOM and select **9:ZoomStat** to resize the window to fit your data. Points on a connected dot graph or histogram are plotted in the listed order.

...graph a linear regression of data

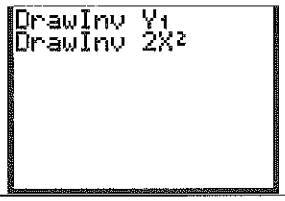
Once you have graphed your data, press STAT and move right to select the **CALC** menu. Select **4:LinReg(ax+b).** Type in the parameters **L1, L2, Y1.** To enter **Y1**, press VARS



and move right to select the **Y-VARS** menu. Select **1:Function** and then **1:Y1**. Press ENTER to display the linear regression equation and Y= to display the function.

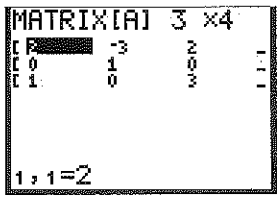
...draw the inverse of a function

Once you have graphed your function, press **DRAW** 2nd PRGM and select **8:DrawInv**. Then enter **Y1** if your function is in **Y1**, or just enter the function itself.



...create a matrix

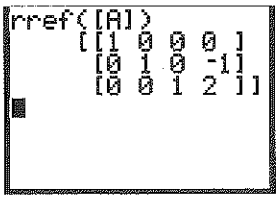
From the home screen, press 2nd x^{-1} to select **MATRX** and move right to select the **EDIT** menu. **Select 1:[A]** and enter the number of rows and the number of columns. Then fill in the matrix by entering a value in each element.



You may move among elements with the arrow keys. When finished, press **QUIT** 2nd MODE to return to the home screen. To insert the matrix into calculations on the home screen, press 2nd x^{-1} to select **MATRX** and select **NAMES** and select **1:[A].**

...solve a system of equations

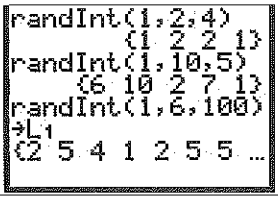
Once you have entered the matrix containing the coefficients of the variables and the constant terms for a particular system, press **MATRX** (2nd x^{-1} , move to **MATH**, and select **B:rref.**



Then enter the name of the matrix and press ENTER. The solution to the system of equations is found in the last column of the matrix.

...generate lists of random integers

From the home screen, press MATH and move left to select the **PRB** menu. Select **5:RandInt** and enter the lower integer bound, the upper integer bound, and the number of trials, separated by



commas, in that order. Press STO× and **L1** to store the generated numbers in **List 1**. Repeat substituting **L2** to store a second set of integers in **List 2.**